

Derive

$$\textcircled{5} \cos(A+B) = \cos A \cos B - \sin A \sin B$$

We know that

$$\cos B = \cos(-B)$$

$$-\sin B = \sin(-B)$$

} In log tables

and that

$$\textcircled{4} \cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\cos(A - (-B)) = \cos A \cos(-B) + \sin A \sin(-B)$$

$$= \cos(A+B) = \cos A \cos B - \sin A \sin B \quad \text{QED}$$

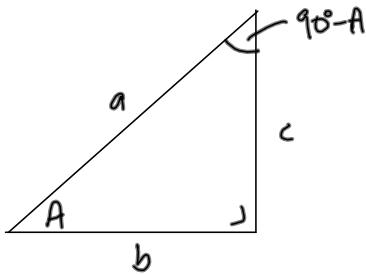
Derive  $\textcircled{6} \cos 2A = \cos^2 A - \sin^2 A$

We know that  $\textcircled{5} \cos(A+B) = \cos A \cos B - \sin A \sin B$

$$\Rightarrow \cos(A+A) = \cos A \cos A - \sin A \sin A$$

$$\cos 2A = \cos^2 A - \sin^2 A \quad \text{QED}$$

Consider



$$\cos A = \frac{b}{a}$$

$$\sin(90^\circ - A) = \frac{b}{a}$$

$$\cos A = \sin(90^\circ - A)$$

likewise:

$$\sin A = \frac{c}{a}$$

$$\cos(90^\circ - A) = \frac{c}{a}$$

$$\sin A = \cos(90^\circ - A)$$

Derive (7)  $\sin(A+B) = \sin A \cos B + \cos A \sin B$ We know that  $\cos(90^\circ - A) = \sin A$ 

$$\sin(90^\circ - A) = \cos A$$

$$\text{and (4) } \cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\cos((90^\circ - A) - B) = \cos(90^\circ - A) \cos B + \sin(90^\circ - A) \sin B$$

$$\cos(90^\circ - (A+B)) = \sin A \cos B + \cos A \sin B$$

$$\sin(A+B) = \text{RHS}$$

QED